

# Math 1431

## Section 16679

Bekki George: rageorge@central.uh.edu

University of Houston

10/17/19

Office Hours: Tuesdays & Thursdays 11:45-12:45  
(also available by appointment)  
Office: 218C PGH

Course webpage: [www.casa.uh.edu](http://www.casa.uh.edu)

# Questions?

# Popper 14

- ① Is  $f(x) = x^3 + 2x - 3$  invertible?

# Popper 14

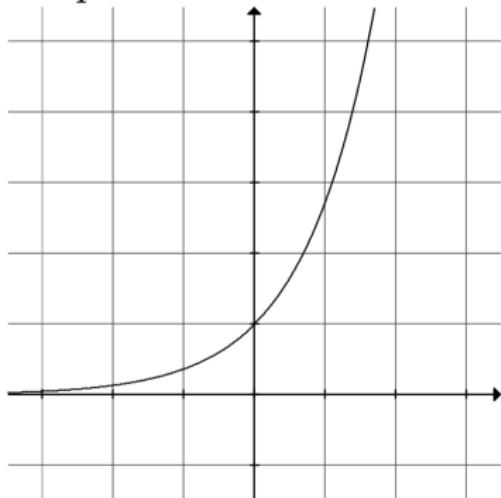
② Find  $(f^{-1})'(2)$  if

$$f(2) = 3, f(4) = 2, f(3) = -2, f'(2) = 7, f'(3) = 5, f'(4) = 10.$$

## Section 4.2 - The Exponential Function

The exponential function:  $f(x) = e^x$  or  $f(x) = \exp(x)$ .

Graph:



## Section 4.2 - The Exponential Function

The derivative of  $f(x) = e^x$  is  $f'(x) = e^x$

Chain rule:  $\frac{d}{dx}e^u = e^u \cdot u'$

## Section 4.2 - The Exponential Function

Examples:

$$\textcircled{1} \quad \frac{d}{dx} e^{2x-1} =$$

$$\textcircled{2} \quad \frac{d}{dx} e^{\sin(x)} =$$

$$\textcircled{3} \quad \frac{d}{dx} e^{x^2 + \sin(x)} =$$

## Section 4.2 - The Exponential Function

Examples:

$$\textcircled{4} \quad \frac{d}{dx} e^{-x^2} =$$

$$\textcircled{5} \quad \frac{d}{dx} \exp\left(-\frac{3}{x}\right) =$$

## Section 4.2 - The Exponential Function

Examples:

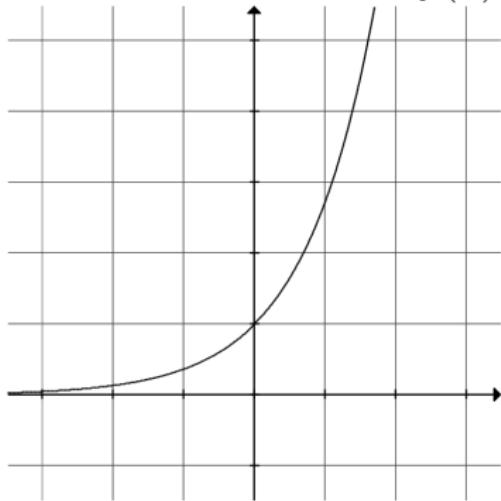
- ⑥ Find the equation of the tangent line to  $y = e^{1-x}$  at the point  $(1, 1)$ .

# Popper 14

- ③ Find  $\frac{d}{dx} \left( e^{\cos(x)} \right)$ .

## Section 4.2 - The Exponential Function

What is the inverse of  $f(x) = e^x$  look like?



Since  $f(x) = e^x$  and  $g(x) = \ln(x)$  are inverses, we have  $e^{\ln(x)} = x$

## Section 4.2 - The Exponential Function

Suppose we want to find the derivative of  $y = 3^x$ . We can re-write this as  $y = e^{\ln(3^x)} = e^{x \ln(3)}$ . Note that  $\ln(3)$  is a constant. Finding  $y'$  we get

Now suppose we want to find the derivative of  $y = a^x$ . Can we find a general formula?

## Section 4.2 - The Exponential Function

Examples:

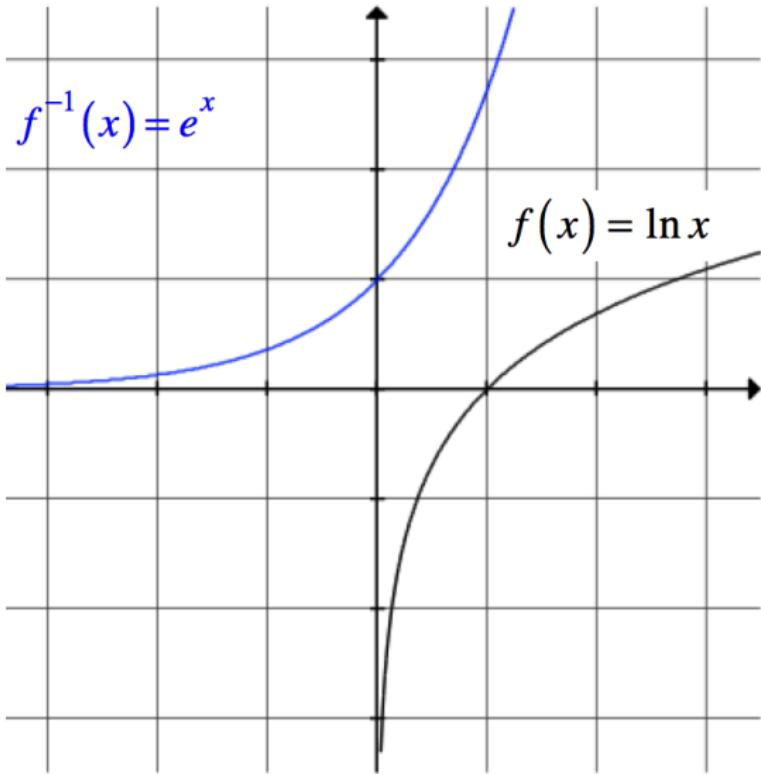
①  $\frac{d}{dx} (2^x) =$

②  $\frac{d}{dx} \left( 5^{3x^2} \right) =$

# Popper 14

- ④ Find  $\frac{d}{dx} (4^x)$ .

## Section 4.3 - Logarithms



$$f(f^{-1}(x)) = x$$

$$f^{-1}(f(x)) = x$$

$$f(e^x) = \ln(e^x) = x$$

$$f^{-1}(\ln x) = e^{\ln x} = x$$

## Section 4.3 - Logarithms

### Properties of Logarithms

Logarithmic form with  $a > 0$ ,  $a \neq 1$ ,  $x > 0$ ,  $y > 0$

i.  $\log_a 1 = 0$

ii.  $\log_a a = 1$

iii.  $a^{\log_a x} = x$

iv.  $\log_a xy = \log_a x + \log_a y$

v.  $\log_a \frac{x}{y} = \log_a x - \log_a y$

vi.  $\log_a x^y = y \log_a x$

Exponential form of a logarithm:

## Section 4.3 - Logarithms

Examples: Expand using properties of logarithms:

$$\textcircled{1} \quad \log_2 \frac{5}{3}$$

$$\textcircled{2} \quad \log_2 \frac{8}{3}$$

$$\textcircled{3} \quad \log_2 \frac{ab}{xy}$$

## Section 4.3 - Logarithms

Natural logs:  $\log_e(x) = \ln(x)$

More examples: Expand using properties of logarithms:

④  $\ln \frac{(x+3)^2}{x\sqrt{x-2}}$

⑤  $\ln \left( \frac{2x^3}{4y^5z^2} \right)$

## Section 4.3 - Logarithms

What is the domain of  $f(x) = \log \sqrt{3 - 4x}$  ?

## Section 4.3 - Logarithms

Graph  $\ln(x) = y$ . What would the derivative look like?

## Section 4.3 - Logarithms

$$\frac{d}{dx}[\ln x] = \frac{1}{x}, \quad x > 0$$

Let  $u$  be a differentiable function of  $x$ . Then,

$$\frac{d}{dx}[\ln u] = \frac{u'}{u}, \quad u > 0$$

Examples:

①  $\frac{d}{dx}[\ln 3x] =$

## Section 4.3 - Logarithms

②  $\frac{d}{dx}[\ln(3x^4 + 5)] =$

③  $\frac{d}{dx}[x^2 \ln x] =$

④  $\frac{d}{dx}[\ln x^4] =$

## Section 4.3 - Logarithms

⑤  $\frac{d}{dx}[(\ln x)^4] =$

⑥  $\frac{d}{dx}[\cos(\ln x)] =$

# Popper 14

⑤  $\frac{d}{dx}(\ln x) =$

# To Do

Read 4.2 and 4.3.

Take quiz 16.

Email me questions if you have any.