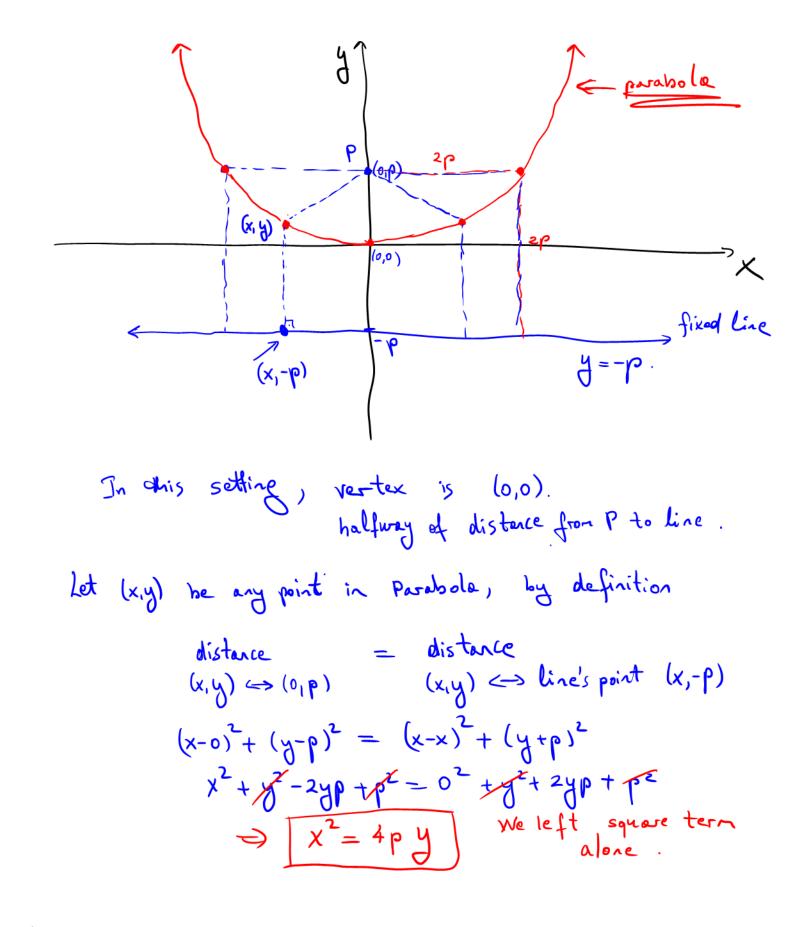
Provodes
$$\subseteq$$
 we visualize $y = x^{1}$
We can have "horizontal" parabolas
but they are not function aryone.
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We can have "horizontal" parabolas
but they are not functions
could open up or down. As we look at conic sections, we saw that the graphs of quadratic functions
could open up or down. As we look at conic sections, we'll see that the graphs of these
second depen up or down. As we look at conic sections, we'll see that the graphs of these
second depen up or down. As we look at conic sections, we'll see that the graphs of these
second depen up or down. As we look at conic sections, we'll see that the graphs of these
second depen up or down. As we look at conic sections, we'll see that the graph of a quadratic function $f(x) = ax^{2} + bx + c$ is a transformation
parabola. But there is more to be learned about parabolas.
 $f(x) = a^{1} + bx + C$
 $\Rightarrow y = a(x-h)^{2} + k$
 $(h,k) = Vertex$
Definition: A parabola is the set of all points equally distant from a fixed line and a
the focus. Understand definitions Part some points = red dot point
 $f(x) = a^{1} + bx + C$
 $2p$
 $parabola = back the distances
form point P and line
 $2p$
 $parabola = back the same .
 $2p$
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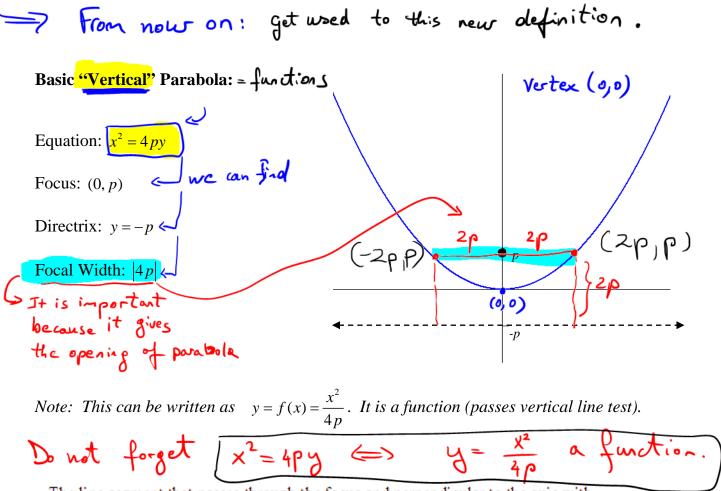
The axis, or axis of symmetry, runs through the focus and is perpendicular to the directrix.

The *vertex* is the point **halfway between** the focus and the directrix.

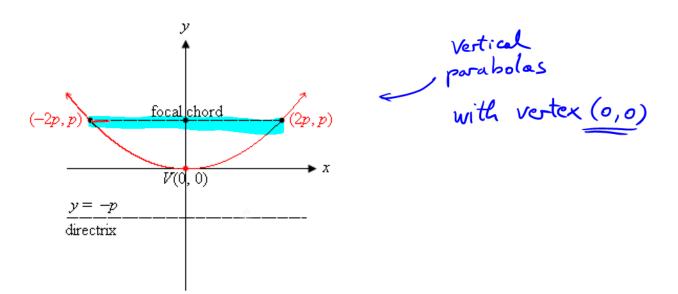
We won't be working with slanted parabolas, just with "horizontal" and "vertical" parabolas.



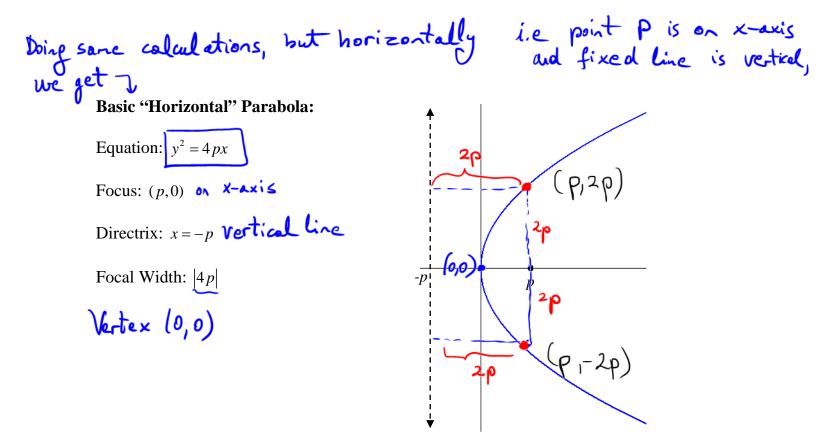
Note: As an exercise, in a similar way, find that formula for horizontal parabolas is y²=4px.



The line segment that passes through the focus and perpendicular to the axis with endpoints on the parabola is called the <u>focal chord</u>. Its length (called the <u>focal width</u>) is 4p.



Example: Graph the parabola $x^2 - 16y = 0$. Steps: () If equation contains x², then it is a vertical parabola. $x^{2}-16y = 0 \iff vertical$ (It is a function $y = \frac{x^{2}}{16}$) (2) Bring it in standard form. x=4py $X^2 = \frac{16}{4}$ 3 Find the focus point 16=4p => p=4 => Focus (0,4) on y-axis. @ give directrix line: y = -p = -4 = y = -4(5) Vertex ↔ (0, 0) 6 Focal width <> 4 p = 44 = 16 2.4 = 8directrix line y=-4 Note: You have this steps for parabolas of vertex (0,0) on page 4.



Note: This is not a function (fails vertical line test). However, the top half $y = \sqrt{x}$ is a function and the bottom half $y = -\sqrt{x}$ is also a function.

Graphing parabolas with vertex at the origin:

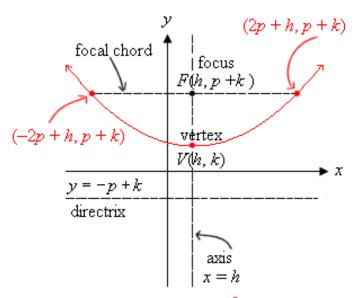
- Look at example D.
- When you have an equation, look for x^2 or y^2
- If it has x^2 , it's a "vertical" parabola. If it has y^2 , it's a "horizontal" parabola.
- Rearrange to look like $y^2 = 4px$ or $x^2 = 4py$. In other words, isolate the squared variable.
- Determine *p*.
- Determine the direction it opens.
 - If *p* is positive, it opens right or up.
 - \circ If p is negative, it opens left or down.
- Starting at the origin, place the focus *p* units to the inside of the parabola. Place the directrix *p* units to the outside of the parabola.
- Use the focal width 4p (2p on each side) to make the parabola the correct width at the focus.

Next time ;

Thursday 09/17

Graphing parabolas with vertex not at the origin:

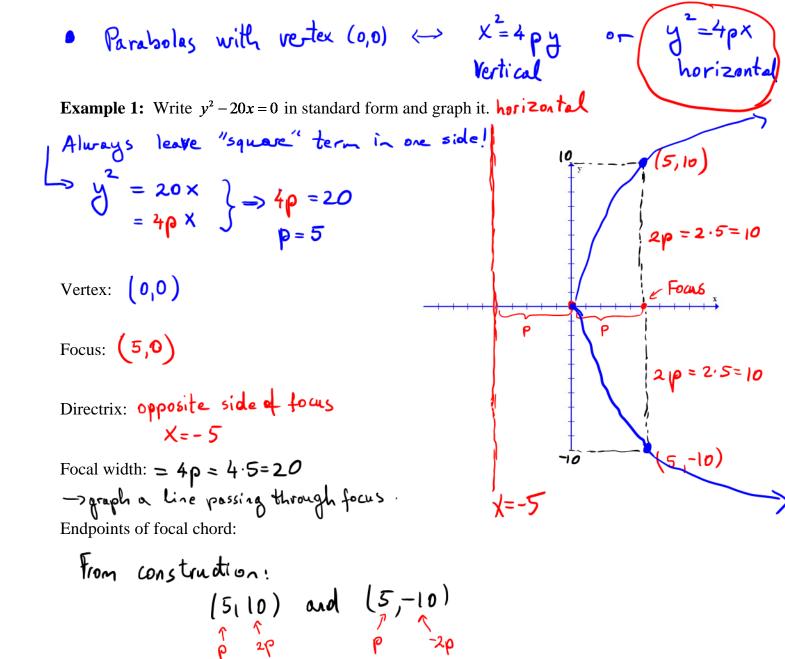
- Rearrange (complete the square) to look like $(y-k)^2 = 4p(x-h)$ or $(x-h)^2 = 4p(y-k)$.
- Vertex is (h,k). Draw it the same way, except start at this vertex.



Graph of the parabola $(x-h)^2 = 4p(y-k)$.

What to keep in mind: • $(y-k)^2 = 4p(x-h) \leftarrow to graph this, is same as y^2 = 4px,$ by shifting the vertex (0,0) to (h, k)

•
$$(x-h)^2 = 4p(y-k) < to graph this, is some as $x^2 = 4px$
by shifting the vertex (0,0) to (h,k).$$



Example 2: Write $6x^2 + 24y = 0$ in standard form and graph it.

$$x = 4gy$$

$$\sum_{k=1}^{n} (x^{2} - \frac{2}{6})$$

$$x^{2} = 4y \Rightarrow 4p = -4 \quad y \text{ Vitical parabola} \\ \Rightarrow p = -1 \quad down ward$$

$$Vertex: (0,0)$$
Focus: (0,-1)
Directrix: $y = +1$
Focal width: $4 \cdot 1 = 4$
Endpoints of focal chord: $(2,-1)$ and $(-2,-1)$

$$\sum_{k=1}^{n} \frac{1}{2} \quad (2,-1)$$
Focus: (0,-1)
Directrix: $y = +1$
Focal width: $4 \cdot 1 = 4$
Endpoints of focal chord: $(2,-1)$ and $(-2,-1)$

$$\sum_{k=1}^{n} \frac{1}{2} \quad (2,-1)$$
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Endpoints of focal chord: $(2,-1)$
Focal width: $4 \cdot 1 = 4$
Endpoints of focal chord: $(2,-1)$
Focal width: $4 \cdot 1 = 4$
Endpoints of focal chord: $(2,-1)$
Focal width: $4 \cdot 1 =$





Example 3: Write $y^2 - 6y = 8x + 7$ in standard form and graph it. herizontal

$$y^{2} - 6y + 1 = 8x + 7 + 1$$

$$(\frac{4}{2} - 3)^{2} = 8(x + 2)$$

$$8 - 4p \Rightarrow p = 2$$

$$y^{2} - 6y + 1 = 8x + 7 + 1$$

$$(\frac{4}{2} - 3)^{2} = 8(x + 2)$$

$$8 - 4p \Rightarrow p = 2$$

$$y^{2} - 8x = 6(x + 2)$$

$$2 \operatorname{left}, 3 \operatorname{up}$$

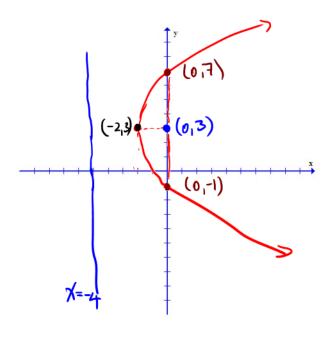
$$(0, 0) \quad \operatorname{Vertex:} (-2, 3) \in \operatorname{opply} \operatorname{shiftments}$$

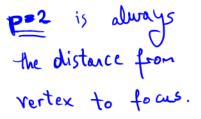
$$(2, 0) \quad \operatorname{Focus:} (0, 3) \in \operatorname{opply} \operatorname{shiftments}$$

$$x = -2 \quad \operatorname{Directrix:} \quad x = -4 \in \operatorname{opply} \operatorname{shiftments}$$

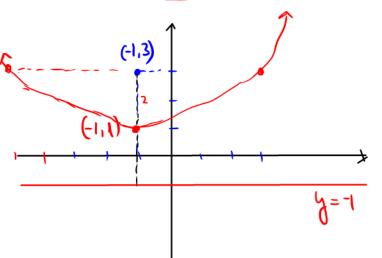
$$42 = 8 \quad \operatorname{Focal} \operatorname{width:} \quad 4 \cdot 2 = 8 \quad \operatorname{some}$$

$$(2, 4) \quad \operatorname{Endpoints} \operatorname{of} \operatorname{focal} \operatorname{chord:} \quad (0, 7) \quad \operatorname{shifted} \quad (0, -1) \quad \operatorname{shifted}$$





Example 5: Suppose you know that the focus of a parabola is (-1, 3) and the directrix is the line y = -1. Write an equation for the parabola in standard form.



=)
$$(x+1)^{2} = 4 \cdot 2(y-1)$$

] $(x+1)^{2} = 8(y-1)$

Having a horizontal directrix line and a focus above it, gives a vertical upward parabola $(x-h)^2 = 4p(y-k)$ Midpoint of distance from focus to line is the vertex = (-1,1) p = distance of focus advertex -2