

Assignment 1: Math 6342 Fall 2018
Professor William Ott

Exercise 1. Let (M, d) be a metric space and let $A \subset M$. Define $\varphi : M \rightarrow \mathbb{R}$ by

$$\varphi(x) = \inf_{a \in A} d(x, a).$$

That is, $\varphi(x)$ is the distance from the point x to the set A . Prove that φ is continuous.

Exercise 2. Exercises from Munkres.

(a) §13 – 3, 5, 6, 8

(b) §16 – 3, 4, 8

(c) §17 – 3, 6, 9, 11, 13, 14, 19(cd), 21