

Math 1432 Spring 2018: Exam 2 Review

Professor William Ott

Exam 2 will cover the material in Sections 5.5, 7.1–7.4, 7.8, 8.1–8.2, 8.3 (moments and centers of mass), and 10.1–10.4 of *Calculus: Early Transcendentals* (Edition 8E) by James Stewart. Possible exercise types include true/false questions, statements of definitions and major results, computational exercises, and exercises requiring theoretical arguments. At least one of the exercises from Section 5 and at least one of the theoretical arguments in Section 4 will appear on Exam 2.

1. DEFINITIONS

You should be able to define and use the following.

- (1) Antiderivative
- (2) Riemann sums, Riemann definite integral
- (3) Indefinite integral
- (4) Arc length function (pg. 547)
- (5) Polar coordinates

2. COMPUTATIONAL TECHNIQUES

- (1) Compute two-sided limits and one-sided limits
- (2) Compute limits at infinity
- (3) Compute derivatives using the differentiation rules (power rule, sum rule, difference rule, constant multiple rule, product rule, quotient rule, chain rule)
- (4) Differentiation of exponential functions, logarithms, trigonometric functions, and inverse trigonometric functions
- (5) Integration techniques
 - Integrands with easily recognizable antiderivatives
 - Substitution
 - Integration by parts
 - Trigonometric integrals (involving sine, cosine, tangent, and secant)
 - Trigonometric substitution (involving sine, cosine, tangent, and secant)
 - Integration of rational functions by partial fraction decomposition (only consider the case of no repeated linear or quadratic factors)
- (6) Compute improper integrals
 - Integrals involving infinite limits of integration ($-\infty$, ∞ , or both)
 - Integrands with a discontinuity at the left or right limit of integration
- (7) Arc length (for curves defined via $y = f(x)$)
- (8) Area of a surface of revolution (Be ready to handle cases such as Gabriel's horn that involve improper integrals.)
- (9) Moments, center of mass
- (10) Parametric curves
 - Be ready to parametrize simple objects such as circles, rays, and line segments.
 - Parametric calculus (tangents to parametric curves, areas, arc length)
- (11) Calculus of polar curves (tangents, areas, arc length)

3. THEORETICAL RESULTS

You should know and be able to apply the following.

- (1) Rolle's theorem, mean value theorem
- (2) Properties of the Riemann integral (see pgs. 385–388)

- (3) Fundamental theorem of calculus, parts I and II
- (4) Symmetry principle (pg. 562)
- (5) Theorem of Pappus (pg. 565)

4. PROOFS/DERIVATIONS

- (1) Theorem of Pappus (pg. 565)
- (2) Derivation of arc length Eq. 3 (pg. 652) from arc length Eq. 2 (pg. 652).

5. SUGGESTED PROBLEMS

Study Assignments 4–6. Focus on exercises that are not too computationally involved and that are at most moderately difficult.