Math 1432 Spring 2018: Exam 3 Review Professor William Ott

Exam 3 will cover the material in Sections 11.1–11.10 of *Calculus: Early Transcendentals* (Edition 8E) by James Stewart. Possible exercise types include true/false questions, statements of definitions and major results, computational exercises, and exercises requiring theoretical arguments. At least one of the exercises from Section 8 and at least one of the theoretical arguments in Section 7 will appear on Exam 3.

1. Definitions (background)

You should be able to define and use the following.

- (1) Antiderivative
- (2) Riemann sums, Riemann definite integral
- (3) Indefinite integral

2. Definitions (specific)

You should be able to define and use the following.

- (1) Sequences
 - Limit of a sequence
 - Convergent sequence, divergent sequence
 - Increasing sequence, decreasing sequence, monotonic sequence
 - Bounded above, bounded below
 - Recursively defined sequence
- (2) Series
 - Sequence of partial sums
 - Convergent series, divergent series
 - Geometric series
 - Harmonic series, *p*-series
 - Alternating series
- (3) Absolute convergence of a series, conditional convergence of a series
- (4) Power series
 - Radius of convergence, interval of convergence
- (5) Taylor series, Maclaurin series
- (6) Taylor polynomial $T_M(x)$

3. Computational techniques (background)

- (1) Compute two-sided limits and one-sided limits
- (2) Compute limits at infinity
- (3) Compute derivatives using the differentiation rules (power rule, sum rule, difference rule, constant multiple rule, product rule, quotient rule, chain rule)
- (4) Differentiation of exponential functions, logarithms, trigonometric functions, and inverse trigonometric functions
- (5) Integration techniques
 - Integrands with easily recognizable antiderivatives
 - Substitution
 - Integration by parts
 - Trigonometric integrals (involving sine, cosine, tangent, and secant)
 - Trigonometric substitution (involving sine, cosine, tangent, and secant)
 - Integration of rational functions by partial fraction decomposition (only consider the case of no repeated linear or quadratic factors)

- (6) Compute improper integrals
 - Integrals involving infinite limits of integration $(-\infty, \infty, \text{ or both})$
 - Integrands with a discontinuity at the left or right limit of integration

4. Computational techniques (specific)

- (1) Compute limits of sequences
- (2) Show that a recursively defined sequence is bounded above and increasing. Find the limit of such a sequence.
- (3) Testing series for convergence/divergence
 - Test for divergence
 - Integral test
 - Comparison test, limit comparison test
 - Alternating series test
 - Ratio test
 - Root test
- (4) Compute the radius and interval of convergence of a power series
- (5) Derive new power series from known power series using the techniques of Section 11.9. Similarly, derive new Taylor/Maclaurin series from known Taylor/Maclaurin series.
- (6) Compute Taylor series/Maclaurin series using the definitions
- (7) Use Taylor series/Maclaurin series to evaluate limits

5. Theoretical results (background)

You should know and be able to apply the following.

- (1) Rolle's theorem, mean value theorem
- (2) Properties of the Riemann integral (see pgs. 385–388)
- (3) Fundamental theorem of calculus, parts I and II

6. Theoretical results (specific)

You should know and be able to apply the following.

- (1) Monotonic sequence theorem (pg. 702)
- (2) If the series $\sum_{n=1}^{\infty} a_n$ converges, then $\lim_{n\to\infty} a_n = 0$.
- (3) Three possible behaviors of a power series (Theorem 4, pg. 749)
- (4) Taylor's theorem (as stated in class)

7. Proofs/Derivations

- (1) If a series $\sum_{i=1}^{\infty} a_i$ is absolutely convergent, then it is convergent.
- (2) If the series $\sum_{n=1}^{\infty} a_n$ converges, then $\lim_{n\to\infty} a_n = 0$.

8. Suggested problems

Study Assignments 7–9. Focus on exercises that are not too computationally involved and that are at most moderately difficult.