

1. Let V and W be vector spaces, and let $T : V \rightarrow W$ be linear. Suppose $\{\mathbf{v}_1, \dots, \mathbf{v}_p\}$ is a linearly dependent subset of V . Prove that $\{T(\mathbf{v}_1), \dots, T(\mathbf{v}_p)\}$ is a linearly dependent subset of W .
2. If $T : \mathbb{R}^2 \rightarrow \mathbb{R}^3$ is linear and $T(1, 1) = (1, 2, 2)$, $T(2, 3) = (2, -1, 2)$, find:
 - (a) $T(1, 0)$ and $T(0, 1)$
 - (b) $T(x, y)$ for any real numbers x and y .